

# **AN OBSTACLE-CONTROLLED CREEP MODEL FOR SN-PB AND SN-BASED LEAD-FREE SOLDERS**

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# Addendum

- **Missing reference in paper:**
  - Shi, X. Q., Wang, Z. P., Zhou, W., Pang, H. L. J. and Yang, Q. J., “A new creep constitutive model for eutectic solder alloy”, *ASME Trans., J. of Electronic Packaging*, June 2002, pp. 85-90
- **References for additional examples in presentation**
  - Lu, W-Y., Lim, T. J., Boyce, B. L., Grazier, J. M., and Fang, H. E., “Small scale multiaxial deformation experiments on solder for high-fidelity model development”, Sandia National Laboratories, SAND Report, SAND2002-8592, December 2002
  - Kim, K. S., Huh, S. H. and Sukanuma, K., "Effects of cooling speed on microstructure and tensile properties of Sn-Ag-Cu alloys", *Materials Science and Engineering A*, Elsevier Science, 2001
- **In the paper, “steady-state” refers to “minimum creep rates”**

# CONTEXT

- **Reliability assessment requires a reasonably accurate description of the thermo-mechanical behavior of lead-free solders.**
- **If we don't understand how solder responds to external loads (thermal or mechanical), how can we interpret or extrapolate accelerated testing results?**
  - At best, thermal cycling profiles are not optimal and lack in efficiency
  - At worse, accelerated testing is equivalent to shooting in the dark.
- **Reliable constitutive models are needed:**
  - For solder joint stress/strain analysis
  - To develop acceleration factors and life prediction models

# ABOUT CLASSICAL APPROACHES TO CREEP OF LEAD-FREE SOLDERS

- **Emphasis has been on “steady state” creep**
- **Primary creep rate models for solders include a time variable (not a recommended practice in constitutive modeling)**
- **Secondary creep stage: its duration is not well defined in test**
  - Reliability models assume that steady state creep can last for ever
- **Tertiary creep has received little attention**
  
- **THIS PRESENTATION FOCUSES ON THE STRESS AND TEMPERATURE DEPENDENCE OF MINIMUM CREEP RATES**

# ABOUT MINIMUM CREEP RATES

- **The application of classical “steady-state” creep models to lead-free solders shows major anomalies.**
  - Power-law creep models give different temperature-dependent stress exponents in low and high stress regions (e.g., Song et al., 2002)
  - Hyperbolic sine creep models have led to widely different activation energies for a given alloy, depending on stress levels and the covered temperature range
- **Recurring theme: parameters of classical “steady-state” creep models are stress- and temperature-dependent**
  - “Something” is not captured in classical steady-state creep models
  - Use them with caution

# What The Experts Say

- ***“DESPITE BEING WIDELY ADOPTED FOR OVER 50 YEARS, POWER-LAW CONCEPTS HAVE NOT LED TO THEORIES WITH VERIFIED PREDICTIVE CAPABILITIES...IT IS, THEREFORE PROPOSED THAT POWER-LAW REPRESENTATION OF STEADY STATE CREEP RATES SHOULD BE ABANDONED...”***

**Wilshire, 2002**

- ***“LACKING ANY PHYSICAL MODEL, IT MUST BE CONSIDERED FORTUITOUS THAT ANY SET OF  $n'$  AND  $\alpha'$ , CAN CORRECTLY DESCRIBE THE BEHAVIOR OVER A WIDE RANGE OF STRESSES”***

**Frost and Ashby, 1982**

- In reference to the “sinh” model constants  $n'$  (exponent) and  $\alpha'$  (“breakdown stress factor”)

# Alternative: Obstacle-Controlled Creep Models

## ● One-cell model:

$$\dot{\varepsilon} = A \sigma^m \cdot \exp\left[-\frac{Q_a}{kT} \left(1 - \frac{\sigma}{\sigma_0}\right)\right]$$

- A first-principle, material-based plasticity model (Ashby & Frost, 1982)

$\sigma_0$  " athermal flow strength = maximum flow strength at 0 K.

- The true activation energy:  $Q = Q_a - V \cdot \sigma$  ( $V = \text{constant}$ ) is stress-dependent
  - Creep is a thermally-activated, stress-aided rate process

## ● Two-cell model:

$$\dot{\varepsilon} = A_1 \sigma^{m_1} \cdot \exp\left[-\frac{Q_{a1}}{kT} \left(1 - \frac{\sigma}{\sigma_{01}}\right)\right] + A_2 \sigma^{m_2} \cdot \exp\left[-\frac{Q_{a2}}{kT} \left(1 - \frac{\sigma}{\sigma_{02}}\right)\right]$$

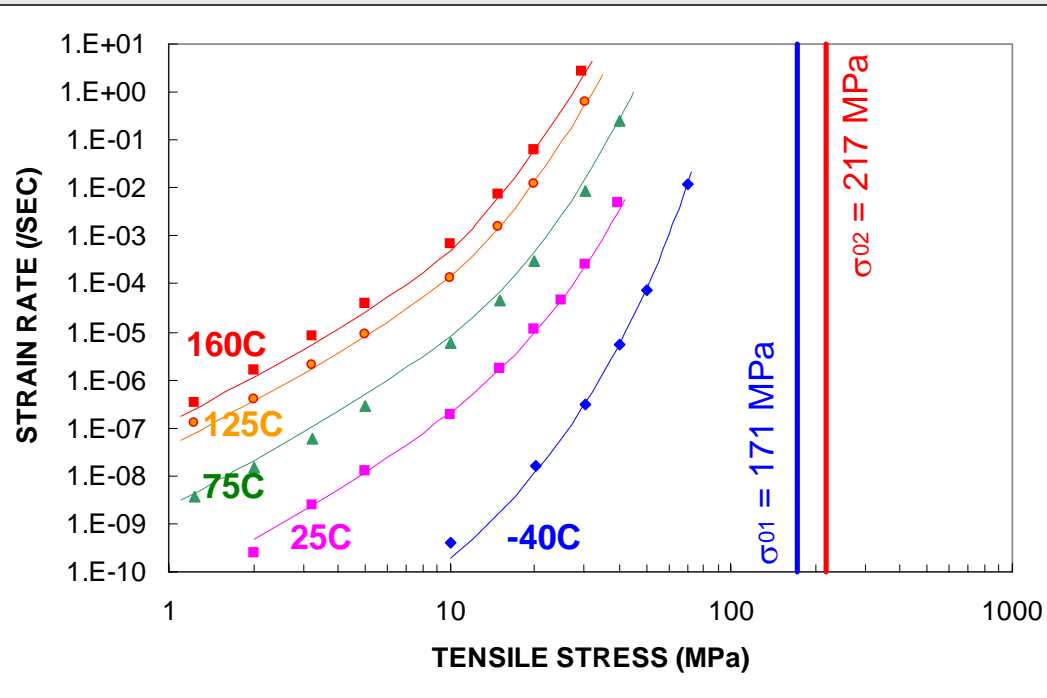
when two creep mechanisms have been identified

# Alternative: Obstacle-Controlled Creep Models (cont'd)

- Paper presents the application of such models to:
  - Near-eutectic SnPb
  - **Seven lead-free solders in the SnAg, SnAgCu, SnBi, SnCu families.**
- Testing of models against independent data and over a wide range of circumstances is a must (for this or other type of model) before models can be applied to real joints.



# Sn37Pb Creep Model



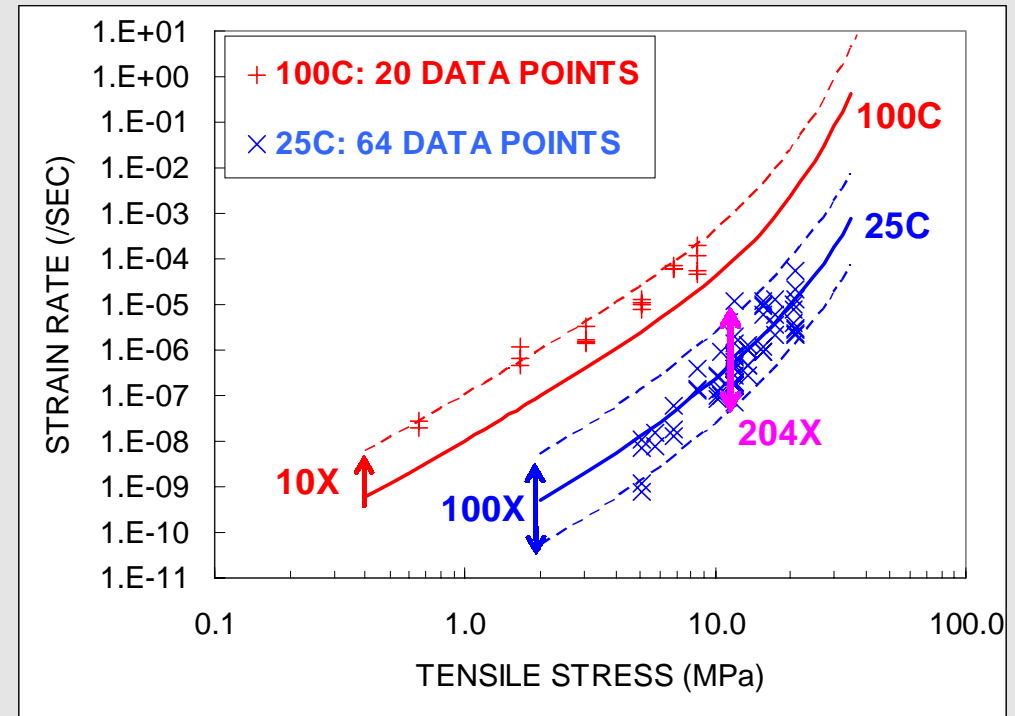
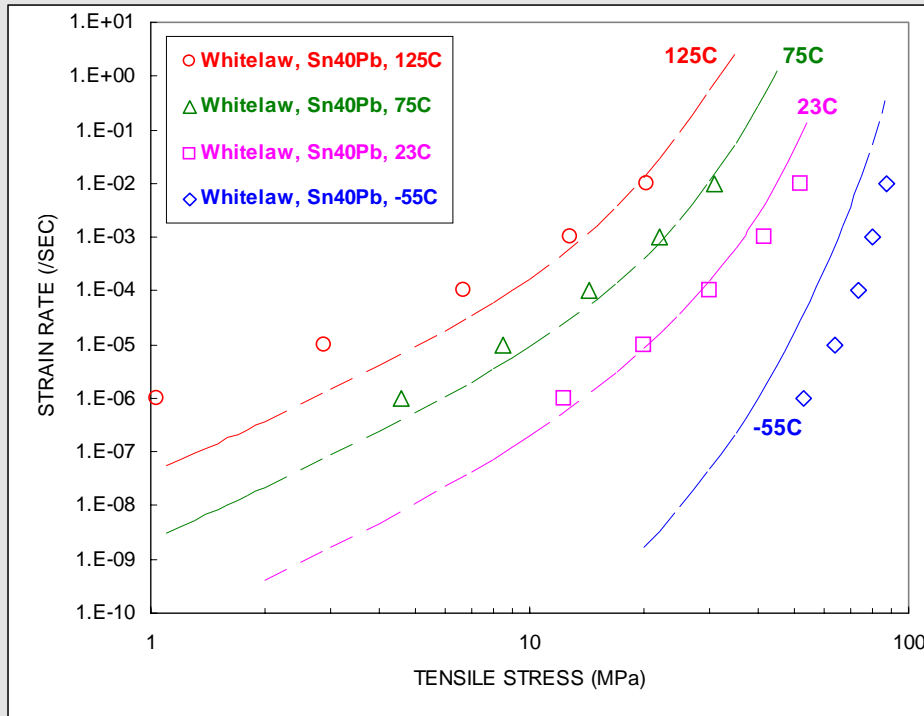
- **Two-cell model for two creep mechanisms**
  - Grain boundary sliding
  - Matrix creep
- **Six test cases**
  - Tensile creep
  - Tensile strength
  - Compressive stress relaxation
  - Thermal cycling hysteresis loop

- **Model after Sn37Pb tensile creep data**

- Data from Shi et al., June 2002, *J. of Electronic Packaging*

$$\dot{\varepsilon} (/ \text{sec}) = 17.4\sigma^{3.07} \cdot \exp\left[-\frac{7988}{T(K)}\left(1-\frac{\sigma}{171}\right)\right] + 5112\sigma^{5.89} \cdot \exp\left[-\frac{13516}{T(K)}\left(1-\frac{\sigma}{217}\right)\right]$$

# SnPb Model Test # 1 & 2: Tensile Creep



- **Sn40Pb tensile data**

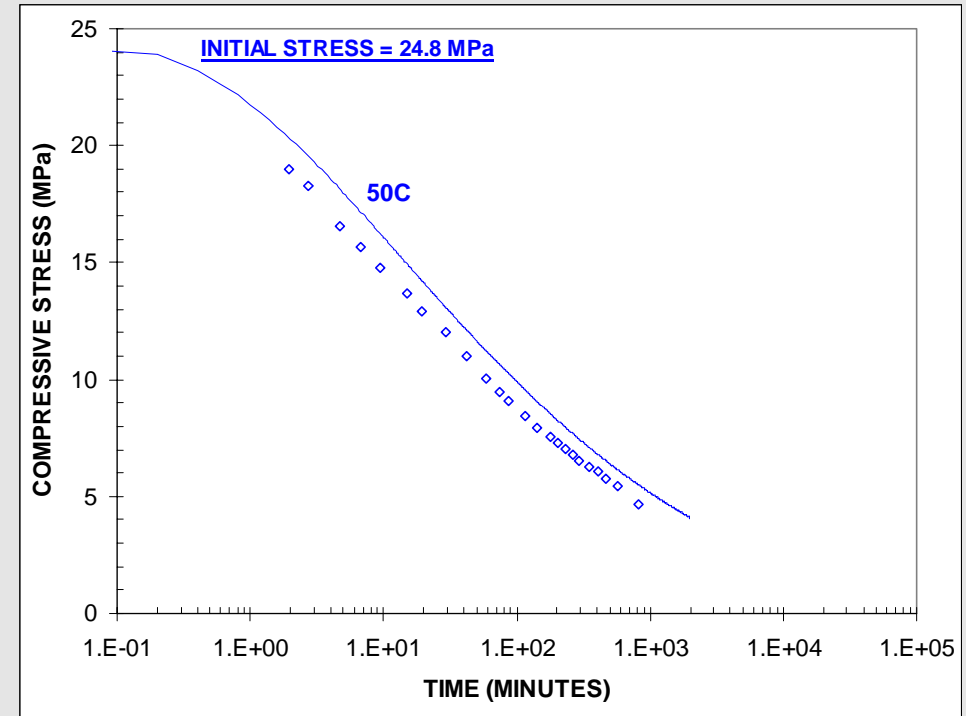
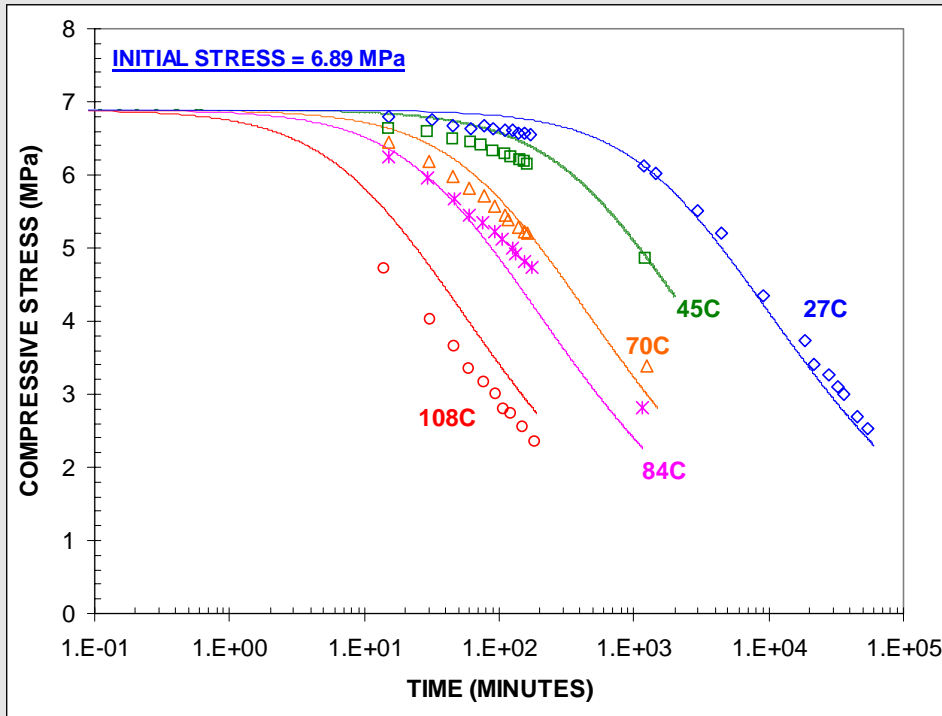
- From Whitelaw et al., 1999

- **Sn37Pb tensile data**

- From Lu et al., 2002, SAND2000-8592 report (Sandia National Laboratories)
- This example is not in the paper
- Model is represented by solid lines

- **Creep rate model with no calibration factor**

# SnPb Model Test # 3: Stress Relaxation Data

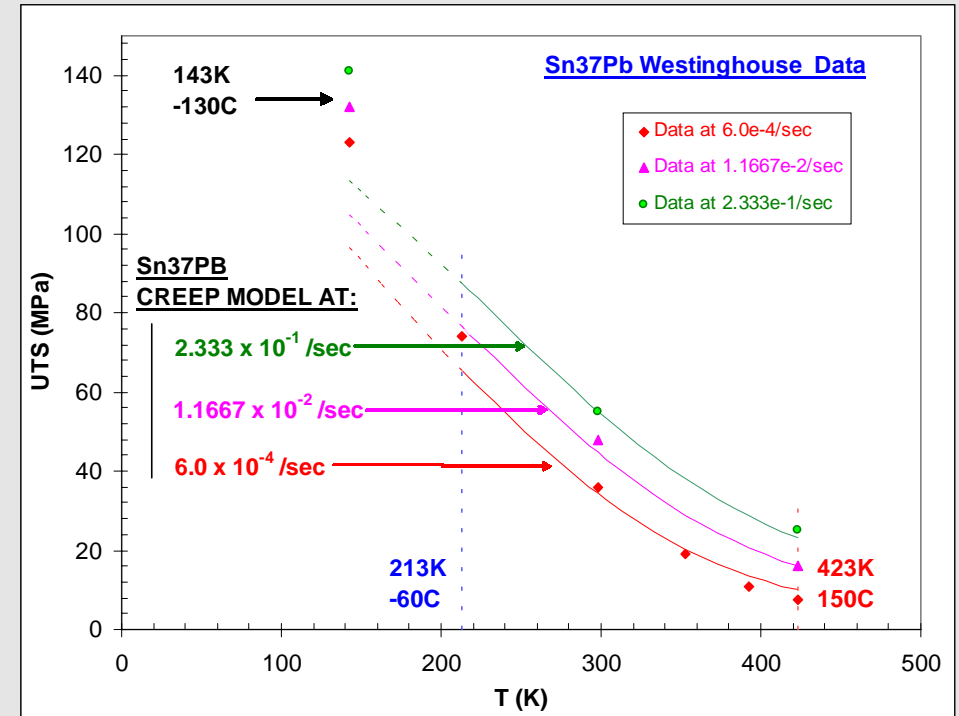
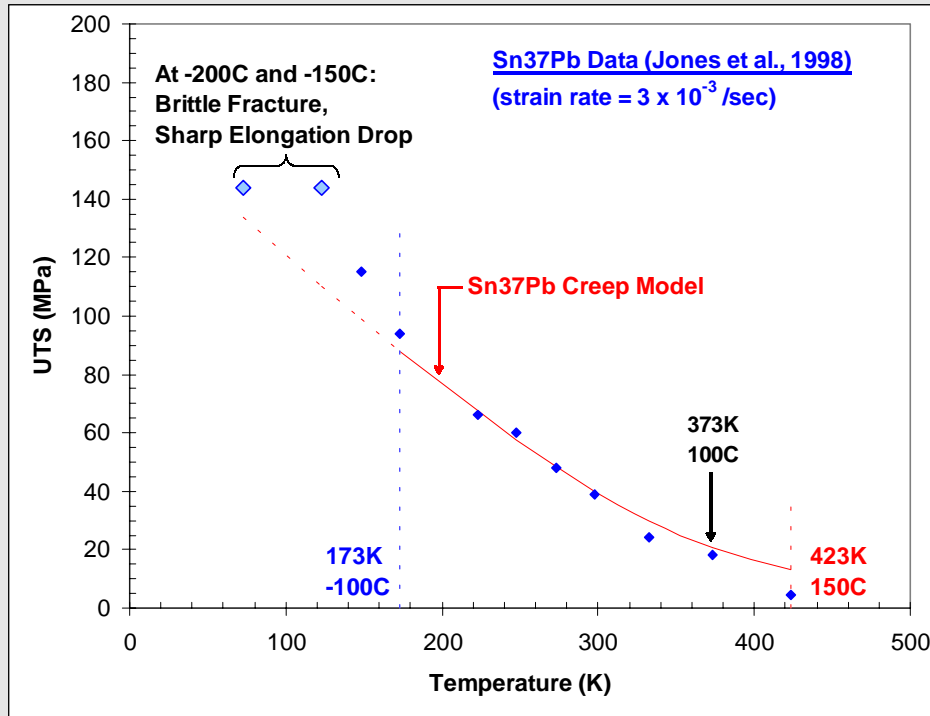


- **Sn40Pb data**

- From Baker et al., 1973
  - Temperature: 27°C to 108°C
  - Initial stress: 6.89 MPa or 24.8 MPa

- **Creep rate model with calibration factor:  $C = 9 \times 10^{-3} \sim 1/100$**

# SnPb Model Test # 4 & 5: Strength Data



- **1 strain rate**

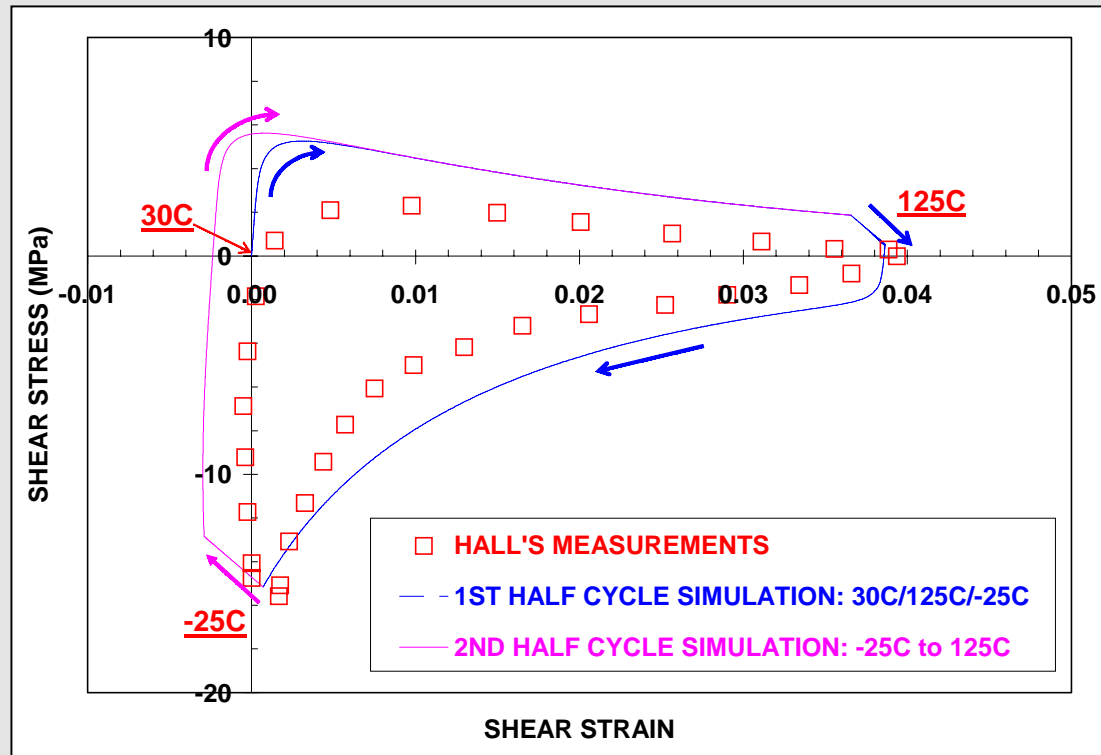
- Temperature: -200°C to 150°C

- **3 strain rates**

- Temperature: -130°C to 150°C

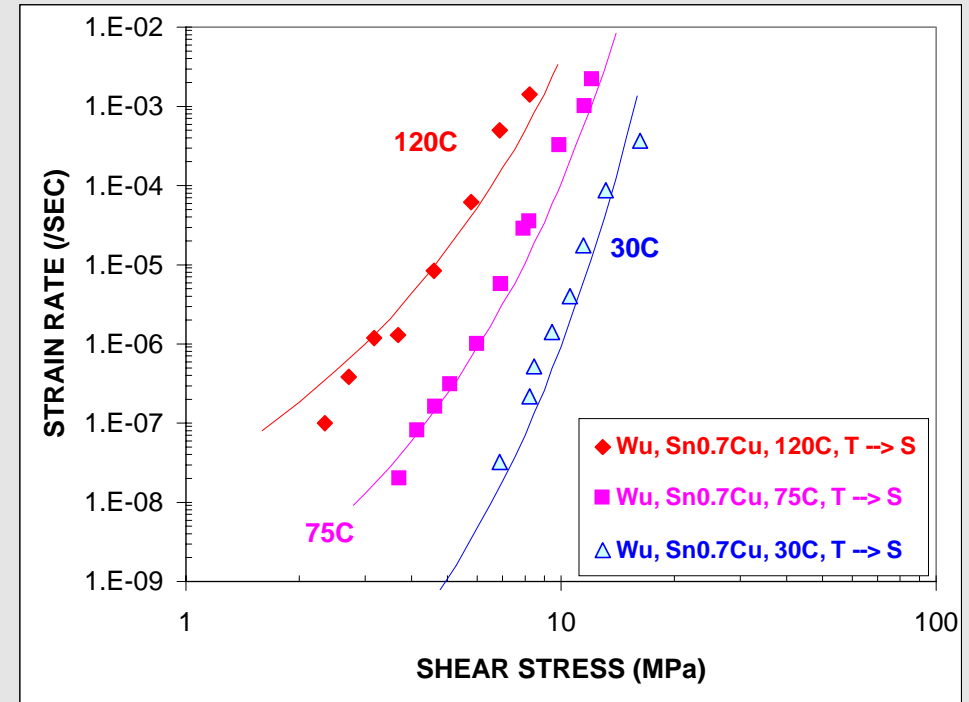
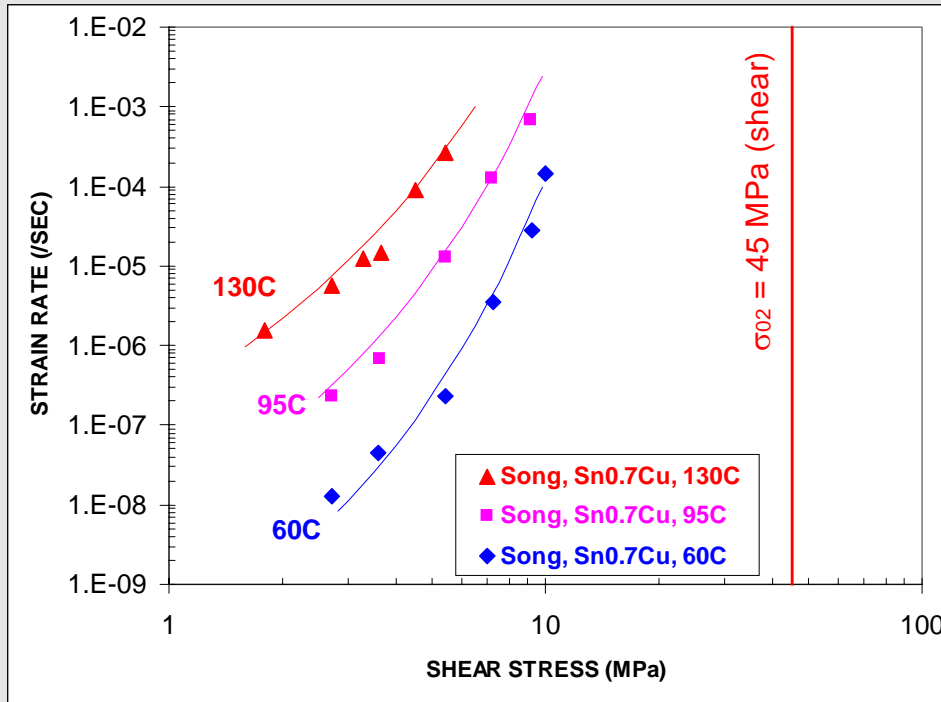
- **Strength (UTS) from creep rate model with no calibration factor**

# SnPb Model Test # 6: Thermal Cycling Hysteresis Loop



- **Sn40Pb data**
  - From Hall, 1984: -25°C to 125°C Thermal Cycling (5 hour ramps, 2 hour dwells)
- **Model lines: elastic deformation + steady-state creep only**
- **Used creep rate model with no calibration factor**

# Sn0.7Cu: One-Cell Creep Model & Model Testing



- **Model after Sn0.7Cu shear creep data**

- From Song et al., 2002a
- One-cell model:

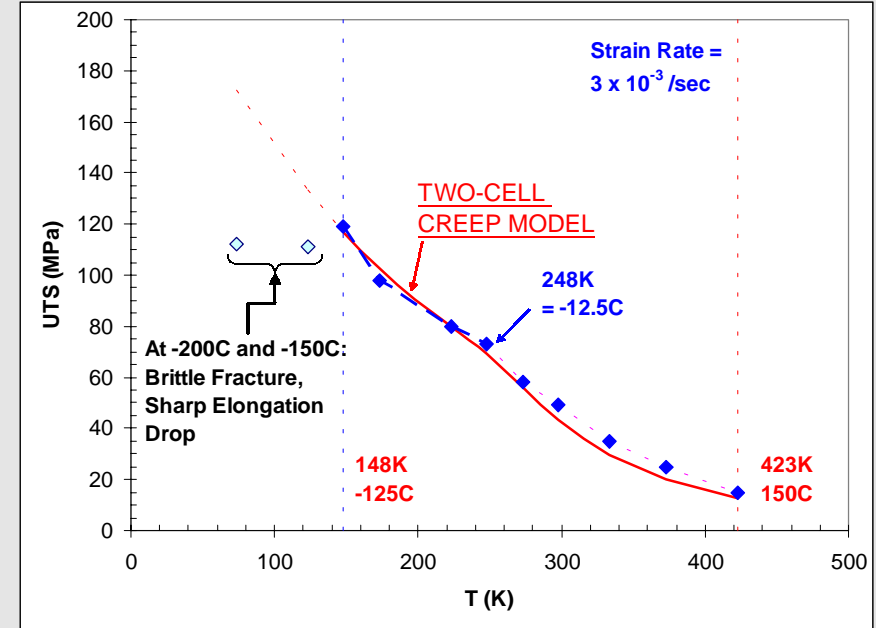
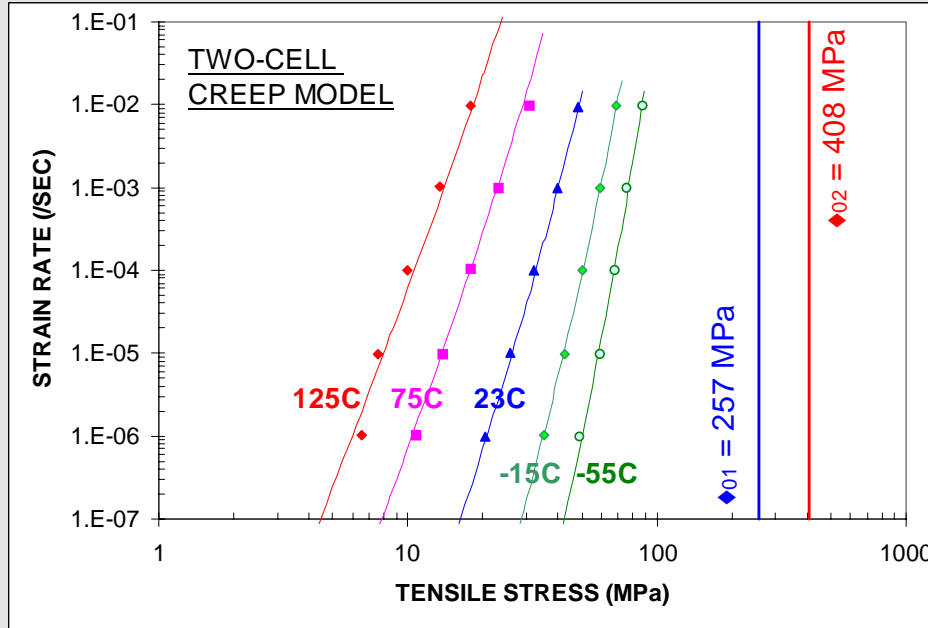
$$\dot{\gamma} (\text{/sec}) = 2.23 \cdot 10^8 \cdot \tau^{2.23} \cdot \exp \left[ -\frac{14235}{T(K)} \left( 1 - \frac{\tau}{45.2} \right) \right]$$

- **Sn0.7Cu tensile creep data**

- From Wu et al., 2002
- Converted to shear (Von Mises)

- **Creep rate model with calibration factor  $C = 0.2$**

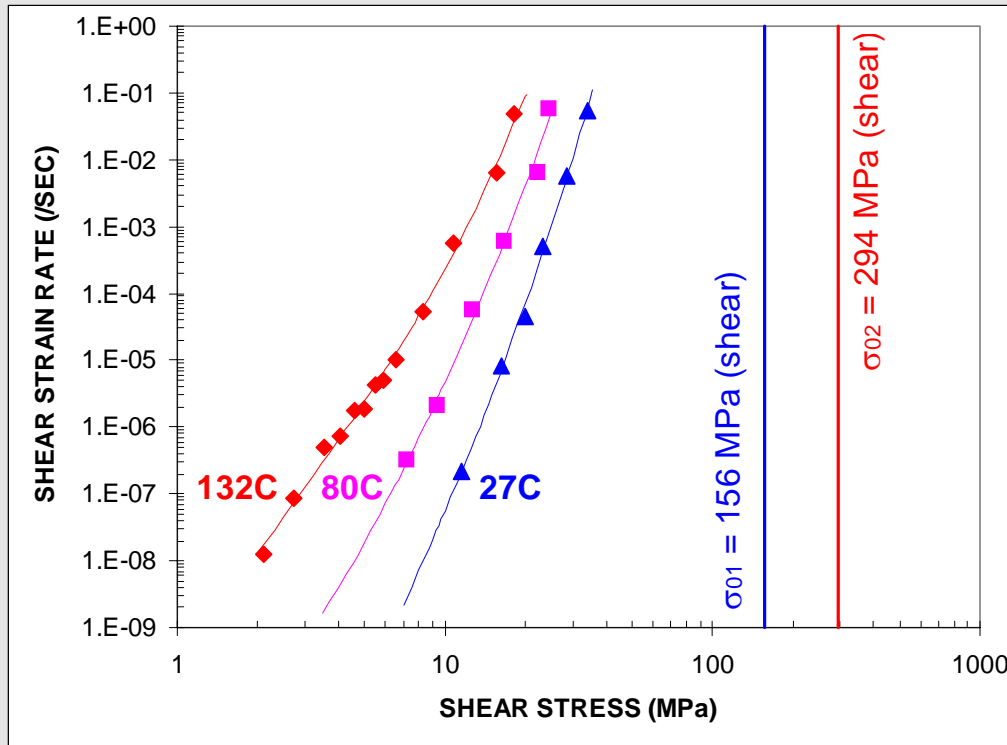
# Sn4.0Ag: Two-Cell Creep Model & Model Testing



- Model after Sn4Ag tensile strain-rate jump creep data
  - From Neu et al., 2001

- Sn4Ag strength data
  - From Jones et al., 1998
- Predicted strength using creep rate model with no calibration factor

# Sn3.5Ag Creep Model

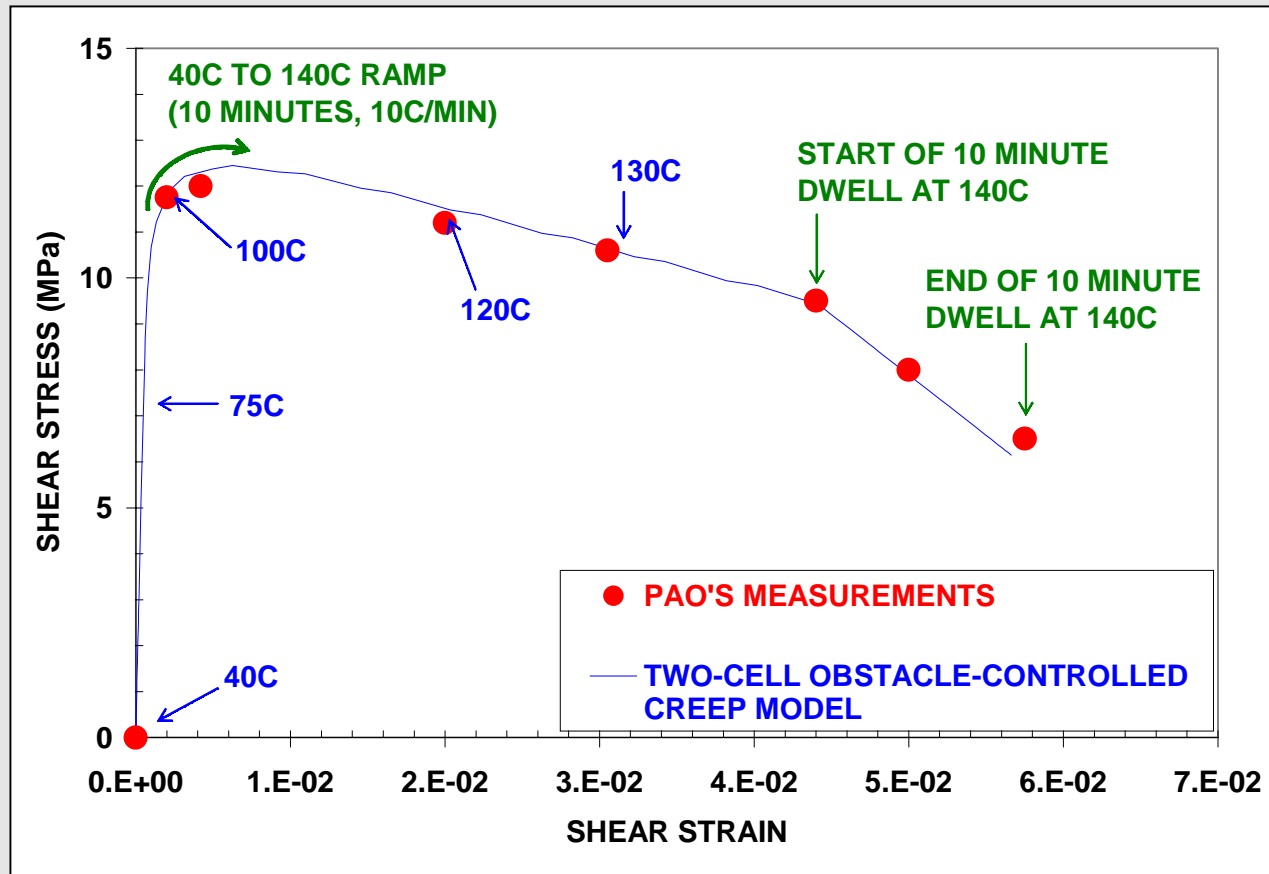


- **Model after Sn3.5Ag shear creep data from shear testing of chip carrier solder joints**
  - From Darveaux et al., 1992

- **Two-cell model based on limited data: 27-132°C**
- **Nine test cases**
  - Tensile creep
  - Tensile strength
  - Compression creep
  - Shear creep (lap joint)
  - Shear creep of flip-chip joints
  - Shear strength
  - Thermal cycling stress/strain cycle
- **Need creep rate calibration factor for 4 test cases**

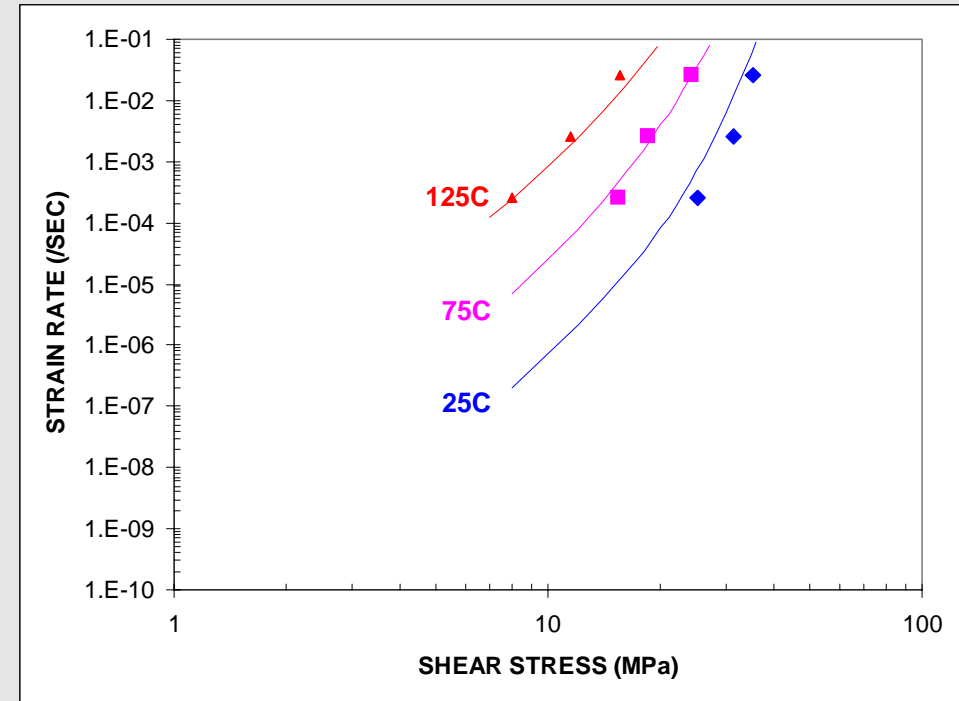
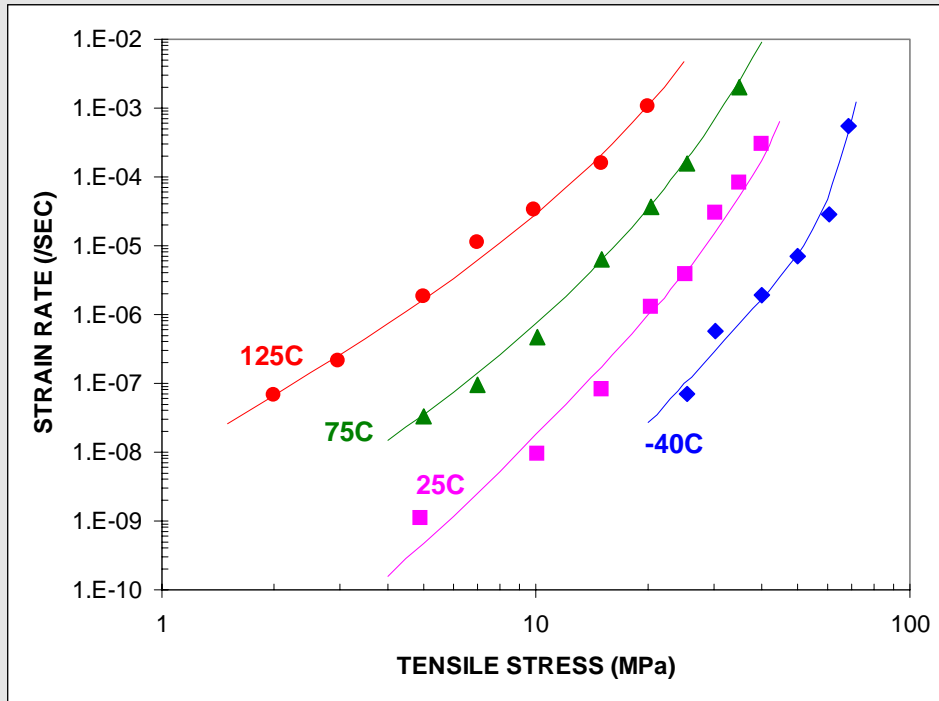


# Sn3.5Ag Model Test: Thermal Cycling Data



- Sn3.5Ag thermal cycling data
  - From Pao, 1997
- Creep rate model with calibration factor  $C = 22$

# Sn3.8Ag0.7Cu Two-Cell Creep Model & Model Testing



- **Model after Sn3.8Ag0.7Cu tensile creep data**

- From Pang et al., 2004

- **Two-cell model**

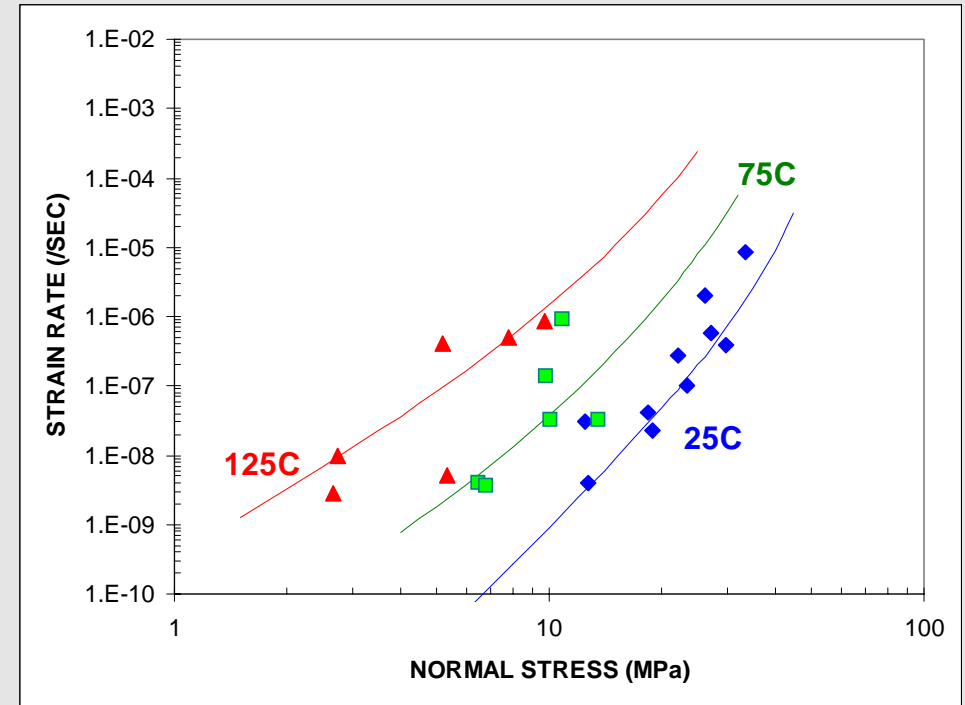
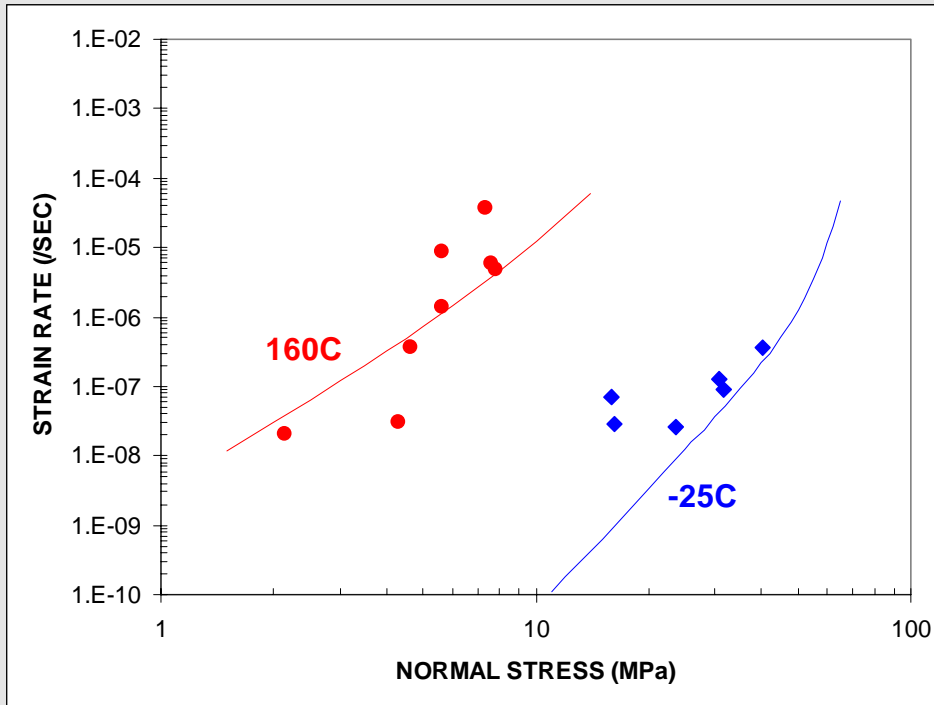
- 5 test cases

- **Sn3.8Ag0.7Cu shear strength data**

- From Pang et al., 2003

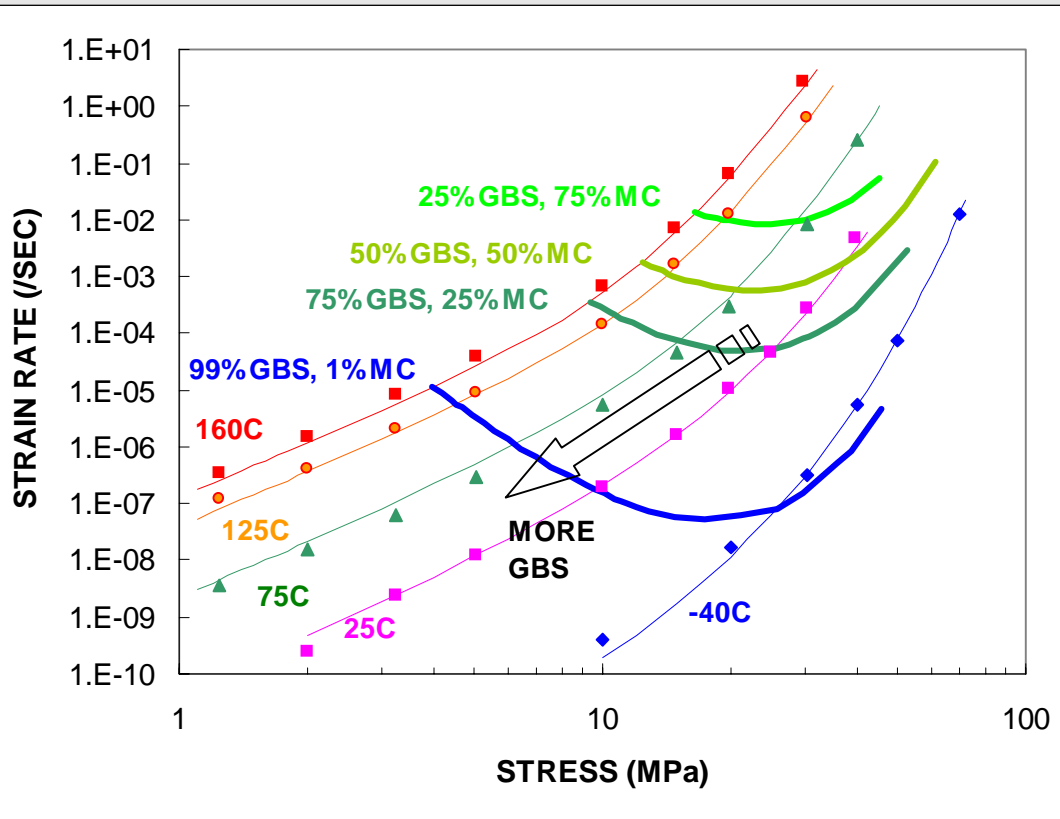
- **From creep rate model with no calibration factor.**

# Sn3.8Ag0.7Cu Model Testing: Comparison to Sn3.9Ag0.6Cu Compression Creep Data



- **Sn3.9Ag0.6Cu compression creep data**
  - From Vianco, 2004
- **Comparison to Sn3.8Ag0.7Cu two-cell model**
  - **With model calibration factor  $C = 0.05$**

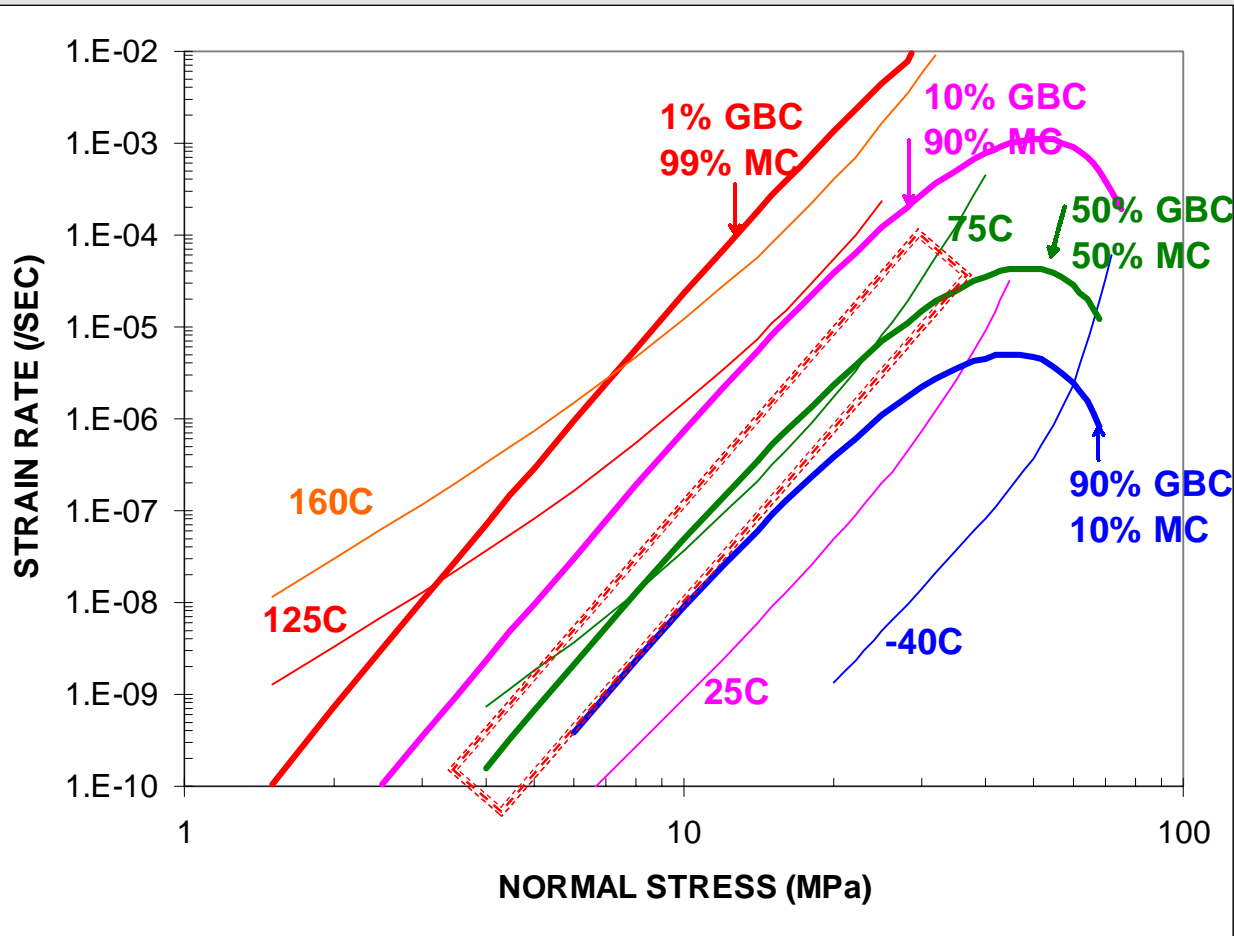
# Sn37Pb Creep Mechanism Contours



- Creep mechanism contour lines predict “75% GBS, 25% MC” transition at stresses < 10 MPa and temperatures from -40°C to 160°C
  - ▮ GBS is dominant mechanism
  - ▮ Agrees with creep contour charts by Grossman, 2002

- Isothermal creep rate lines as in Slide # 9
- GBS = Grain Boundary Sliding; MC = Matrix Creep

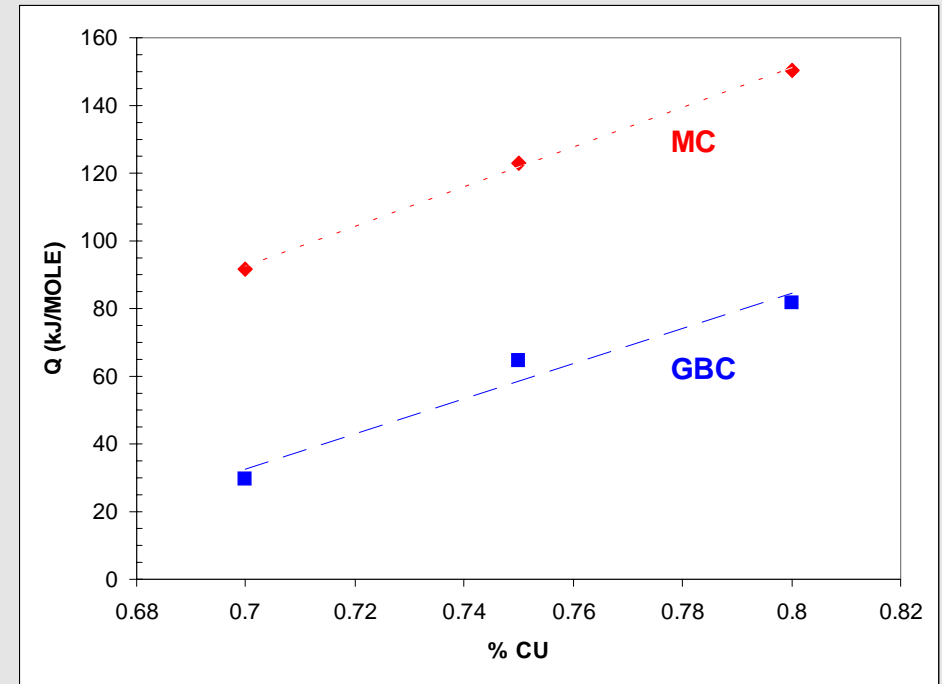
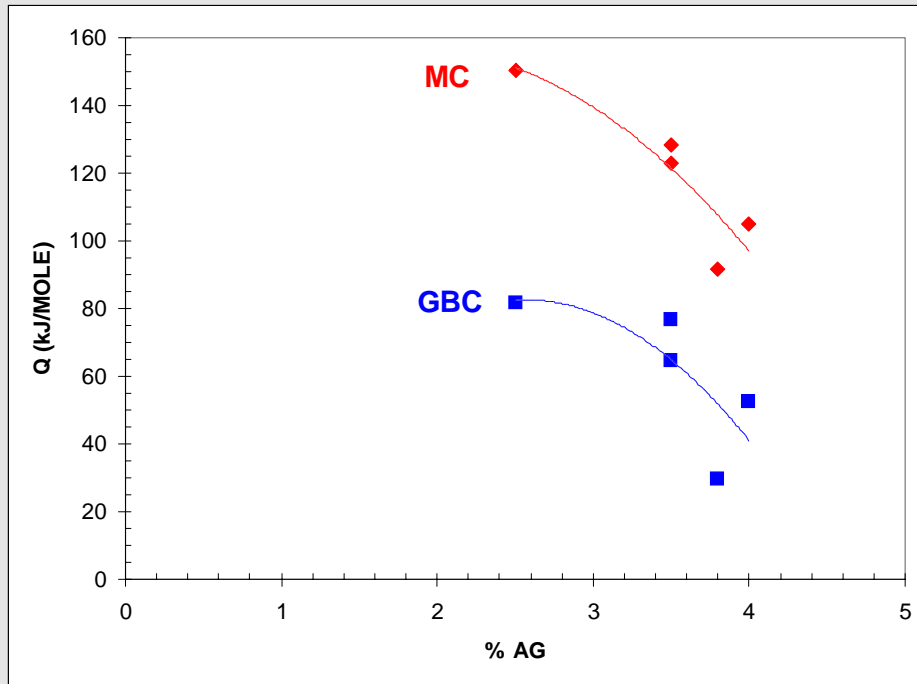
# Sn3.9Ag0.6Cu Creep Mechanism Contours: A Very Different Pattern



- Creep mechanism contour lines predict “50% GBC, 50% MC” transition at about 75°C (for stresses below 30 MPa)
- Agrees with creep rate and micro-structural analysis by Vianco, 2004

- Isothermal creep rate lines with calibration factor ( $C = 0.05$ ) to match Sn3.9Ag0.6Cu compression creep data as in slide # 19

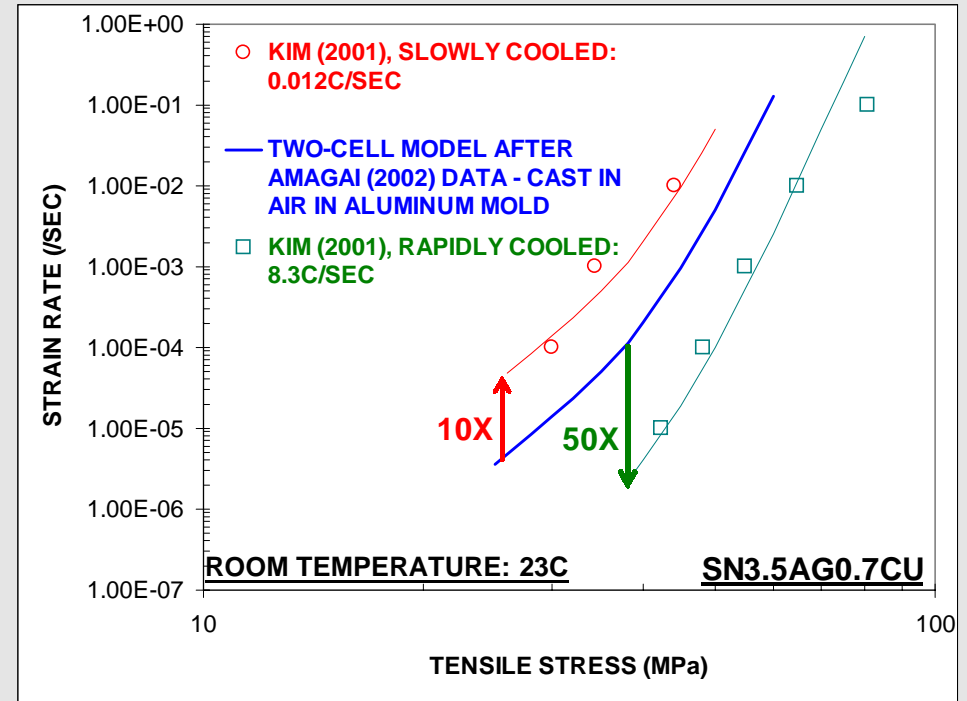
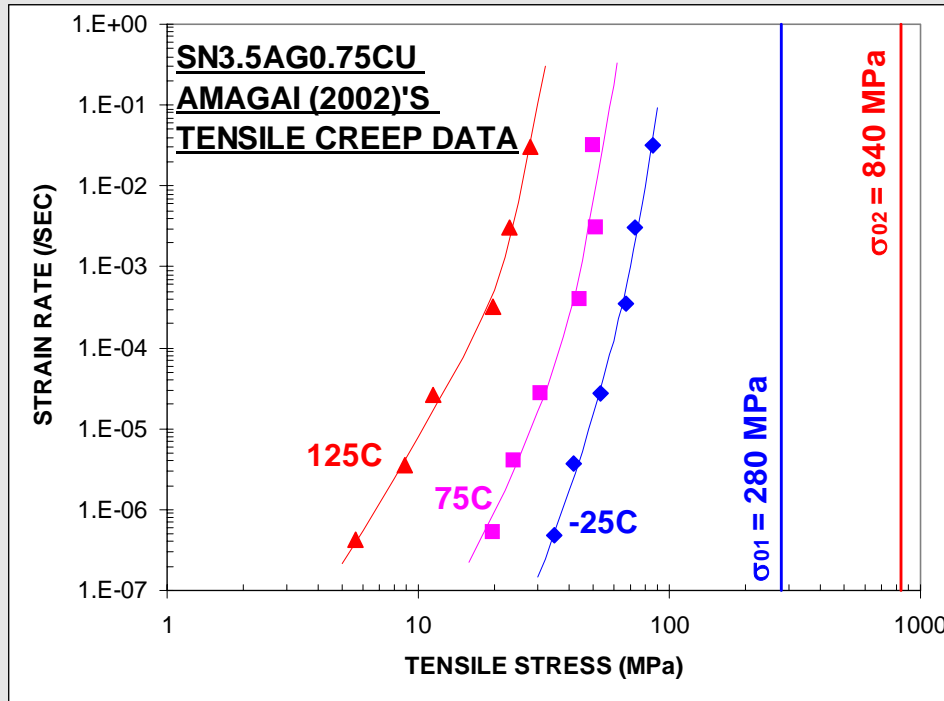
# Effect of Alloy Composition on Creep Activation Energy



- Effect of **%wt. Ag** (range 2.5-4.0%) on apparent creep activation energies of Sn-Ag and Sn-Ag-Cu alloys

- Effect of **%wt. Cu** (range 0.7-0.8%) on creep activation energies of Sn-Ag-Cu alloys
  - There may be %wt. Ag confounding effects

# What About Calibration Factors?



- Sn3.5Ag0.7Cu creep model: data for ingot air-cooled in Aluminum mold
- Compare creep model to Sn3.5Ag0.75Cu strength data:
  - C = 10 for slowly cooled samples
  - C = 1/50 for rapidly-cooled samples
- Calibration Factors (CFs) depend on many factors: microstructure, specimen size ....
  - Example to the right shows that CFs are dependent on cooling rate.

# Conclusions

- The application of classical creep models to lead-free solders has led to many anomalies
- The obstacle-based creep models offer a promising alternative to describe the stress and temperature dependence of **minimum creep rates** of lead-free solders
  - Models should be fit to creep data covering the largest temperature range of interest (e.g. -55°C to 160°C for SnAgCu)
- **Whatever model is used, test it against many independent results**
  - Verify model applicability to real solder joints.
  - Calibration factors may be needed.
- **Primary and tertiary creep of lead-free solders deserve as much attention**



**THANK YOU FOR YOUR ATTENTION**

**QUESTIONS OR COMMENTS?**